

Pre-Calculus CP 1 – Section 7.3 Notes
Solving Systems of Equations with THREE unknowns

Name: KEY

Ex 1: Super EASY!

$$\begin{aligned} 2x - y + 5z &= 24 \\ y + 2z &= 4 \\ z &= 4 \end{aligned}$$

$y + 2(4) = 4$
 $y = -4$

$2x - (-4) + 5(4) = 24$
 $2x + 24 = 24$
 $2x = 0$
 $x = 0$

$(0, -4, 4)$
↑ ↑ ↑
x, y, z

Ex. 2: Moderately more difficult

a)

$$\begin{aligned} x + y + z &= 6 \\ 2x - y + z &= 3 \\ 3x - z &= 0 \end{aligned}$$

$z = 3x$

$x + y + 3x = 6$
 $4x + y = 6$ *

$2x - y + 3x = 3$
 $5x - y = 3$ *

$+ (4x + y = 6)$ *

$9x = 9$
 $x = 1$
 $z = 3(1) = 3$
 $4(1) + y = 6$
 $y = 2$

$(1, 2, 3)$

b)

$$\begin{aligned} 6y + 4z &= -12 \\ 5x + 3y &= 4 \\ 3y - 4z &= 4 \end{aligned}$$

$6y + 4z = -12$
 $+ (3y - 4z = 4)$

$9y = -8$
 $y = -8/9$

$5x + 3(-8/9) = 4$
 $5x - 8/3 = 12/3$
 $5x = 20/3$
 $x = \frac{20}{15} = \frac{4}{3}$

$6(-8/9) + 4z = -12$
 $-\frac{16}{3} + 4z = -\frac{36}{3}$
 $4z = -\frac{20}{3}$
 $z = -\frac{20}{12} = -\frac{5}{3}$

$(\frac{4}{3}, -\frac{8}{9}, -\frac{5}{3})$

Ex. 3: Difficult- lots of steps!

a)
$$\begin{aligned} 2x + 4y + z &= 1 \\ x - 2y - 3z &= 2 \\ x + y - z &= -1 \end{aligned}$$

$$x = z - y - 1$$

$$2(z-y-1) + 4y + z = 1$$
$$2z - 2y - 2 + 4y + z = 1$$
$$2y + 3z = 3 \quad \checkmark$$

$$\begin{aligned} z - y - 1 - 2y - 3z &= 2 \\ -3y - 2z &= 3 \quad * \end{aligned}$$

$$\begin{array}{r} 2x + 6y + 9z = 9 \\ -2x + (-6y - 4z) = 6 \hline \end{array}$$

$$5z = 15$$

$$z = 3$$

$$2y + 3(3) = 3$$

$$2y = -6$$

$$y = -3$$

$$x = 3 - (-3) - 1 = 5$$

$$(5, -3, 3)$$

b) $x + 2y - 7z = -4 \rightarrow x = -2y + 7z - 4$

$$2x + y + z = 13$$

$$\begin{array}{l} 2x + y + z = 13 \\ 3x + 9y - 36z = -33 \end{array} \rightarrow x + 3y - 12z = -11$$

$$5x + 9y - 36z = -33 \rightarrow -(x + 2y - 7z = -4)$$

$$y - 5z = -7$$

$$2(-2y + 7z - 4) + y + z = 13$$

$$-4y + 14z - 8 + y + z = 13$$

$$-3y + 15z = 21$$

$$-y + 5z = ?$$

$$+ (y - 5z = -7)$$

$$0 = 0$$

infinite solutions

Application

A small corporation borrowed \$775,000 to expand its clothing line. Some of the money was borrowed at 8%, some at 9%, and some at 10%. How much was borrowed at each rate if the annual interest owed was \$67,500 and the amount borrowed at 8% was four times the amount borrowed at 10%?

$$0.08x + 0.09y + 0.10z = 67,500$$

$$x + y + z = 775,000$$

$$x = 4z$$

$$0.08(4z) + 0.09y + 0.10z = 67,500$$

$$0.32z + 0.09y + 0.10z = 67,500$$

$$0.09y + 0.42z = 67,500$$

$$\textcircled{A} \quad 9y + 42z = 6,750,000$$

$$4z + y + z = 775,000$$

$$y + 5z = 775,000$$

$$y = 775,000 - 5z$$

$$\rightarrow 9(775,000 - 5z) + 42z = 6,750,000$$

$$6,975,000 - 45z + 42z = 6,750,000$$

$$225,000 = 3z$$

$$z = \$75,000 @ 10\%$$

$$x = \$300,000 @ 8\%$$

$$y = \$400,000 @ 9\%$$

Homework: p. 527, #1a, 5, 13, 15, 43